

Topic: Transformations of graphs

What is it? Shifting, stretching, shrinking, and reflecting of graphs

Types:

Vertical or Horizontal shift

Reflection

Vertical Stretch or Shrink

Add outside $y = 2^x + 3$
MOVES UP

Subtract outside $y = 2^x - 3$
MOVES DOWN

Add inside $y = 2^{(x+3)}$
MOVES Left

Subtract inside $y = 2^{(x-3)}$
MOVES Right

Multiply by a negative (-) $y = -2^x$

Causes the graph to Flip

Exp: *Reflection over the asymptote*

Linear: *Reflection over the x-axis*

Multiply by a fraction (less than 1) $y = \frac{1}{4}(2)^x$

Causes the graph to Shrink

Multiply by an integer $y = 4(2)^x$

Causes the graph to Stretch

Examples

W

D

H

Z

W

T

A

L

$$\textcircled{1} f(x) = \underline{\underline{2}} \underline{\underline{x}} + \underline{\underline{4}}$$

Parent function $f(x) = x$

- stretch
- up 4

$$\textcircled{2} f(x) = \underline{\underline{2}}^x - \underline{\underline{6}}$$

Parent function $f(x) = 2^x$

- Down 6

$$\textcircled{3} f(x) = \underline{\underline{-\frac{1}{3}}} \underline{\underline{(2)}}^x$$

Parent function $f(x) = 2^x$

- Flip/Reflect
- Shrink

$$\textcircled{4} f(x) = \underline{\underline{3}}^{x+2}$$

Parent function $f(x) = 3^x$

- left 2

$$\textcircled{5} f(x) = \underline{\underline{5}} \underline{\underline{(3)}}^{x-4} + \underline{\underline{2}}$$

Parent function $f(x) = 3^x$

- stretch
- right 4
- up 2

$$\textcircled{6} f(x) = \underline{\underline{-\frac{1}{2}}} \underline{\underline{(4)}}^{x+1} - \underline{\underline{7}}$$

Parent function $f(x) = 4^x$

- Flip/Reflect
- Shrink
- left 1
- down 7